

# The Analysis of Optimal Portfolio Using Single Index Model, The Case of Stocks Listed In Jakarta Islamic Index 2010-2013

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**Abstract**— *The purpose of this study is to apply the single index model in order to make an optimal portfolio for stocks listed in Jakarta Islamic Index (JII). The model is used in order to analyze what stocks to be chosen as components of a portfolio stock and how much proportion to be invested in each stock. This research use stocks that are listed in Jakarta Islamic Index. The reason for choosing stocks listed in JII is because many Indonesians, mostly Muslims, still not familiar with the stock that is accordance with the requirement of Sharia. The data use in this study is secondary data, among others: quarterly stock price data during period of 2010-2013, composite index, interest rate. Sample in this study are 28 companies' stocks listed in the Jakarta Islamic Index, two companies' stock did not meet the criteria of the sample because the companies start listed in the index in 2012. Data analysis methods use in this study are: stocks' return and expected return, stocks' risk, market's return and risk, beta and alpha, variance of residual error, rate of excess return to beta, determine the cut off rate, proportion of fund invested in optimal portfolio, and risk of optimal portfolio. Result of this study showed that there are 10 stocks that meet the criteria of optimal portfolio formation. Those stocks and their proportion are: 24,852% stock of JMSR, 16,587% stock of ASRI, 14,721% stock of INDF, 15,398% stock of AKRA, 11,835% stock of LPKR, 5,684% EXCL, 5,184% MAPI, 3,143% CPIN, 1,511% SMGR and 1,086% stock of KLBF. Based on the calculation, the portfolio's expected return is 10,33% and the risk is 2,74%.*

**Keywords**— *co Optimal Portfolio, Single Index Model, Jakarta Islamic Index*

## I. INTRODUCTION

One of the reasons why investors invest in stocks is to get a good expected rate of return on the stocks they bought. By investing in stocks investors will be exposed to expected return as well as risk. The yield from investing in stocks consists of dividend yield and capital gains yield. In order to reduce the risk of investment, the investors can invest in portfolio of stocks. By investing in stock portfolio means that the investors have to decide how much allocation of fund they will put in each of stocks in the portfolio and they also have to choose which stocks they buy.

Portfolio is a combination of various investment instruments ([9], 2011:1). Portfolio return is the difference between the market value of the portfolio at the end of the period and the beginning of the period plus dividends from stocks in the portfolio received during the observation period, then divided by the value of the initial investment ([9], 2011:10). Investment risk can be minimized through the establishment of an efficient portfolio, so the risk is lower than the risk of each investment instrument (eg shares) that make up the portfolio ([9], 2011:19).

Rational investors' steps in making investment decision are: make analysis of current situation, design optimal portfolio, make investment policy, make investment strategy, monitor and supervise performance the fund manager ([6] 2000).

Indonesia as the biggest Muslim country in the world is holds an enormous market for the development of sharia finance industry. Sharia capital market, which is part of the Sharia finance industry, has an important role in increasing the market share of Sharia finance industry in Indonesia. Although its development is still new compared to the Sharia banking, Indonesia's sharia capital market is expected experience rapid growth along with significant growth in Indonesian capital Market Industry ([www.idx.co.id](http://www.idx.co.id)). On July 3<sup>rd</sup> 2000 The Jakarta Stock Exchange (JSX) has issued the Jakarta Islamic Index. This index is expected to attract Muslim investors to invest in stock exchange market. This is the reason why the stocks in the JII are chosen in this study.

Based on the reason mentioned above, this research is focusing on: The Analysis of Optimal Portfolio Using Single Index Model, The Case of Stocks Listed in The Jakarta Islamic Index 2010-2013

### **Problem's Formulation and objective**

Research problem's formulation in this study is: how to make optimal portfolio of stocks that are listed in the Jakarta Islamic Index using single index model, period 2010 until 2013.

The purpose of this study is to make optimal portfolio of stocks that are listed in the Jakarta Islamic Index using single index model, period 2010 until 2013.

### Research Scope

The research scope of this study is the stock that listed in the Jakarta Islamic Index during the period of 2010 until 2013. The data use in this study is secondary data. The data use are: quarterly stock price data during period of 2010-2013, composite index, interest rate.

### Theoretical Frameworks

Stock return consists of capital gain yield and a dividend yield. Capital gain yield is the difference between the selling price and the purchase price per share divided by purchase price of the share, and the dividend yield is dividend per share divided by the stock purchase price per share, [9] (2011:4) . Return can be divided into: realization return, i.e. the return that has already happened and expected return, i.e. the expected return will be earned by investors in the future.

Risk is defined as the difference between the expected return and its realization. The greater the deviation, the higher the risk , return and investment risk are two words that can not be separated, [9] (2011:19). Risk can be divided into: systematic risk and unsystematic risk. Systematic Risk is a risk that cannot be eliminated by diversification. This risk is influenced by fluctuations in macro factors that can affect the overall market, such as changes in economic and political conditions, taxation, government policies, and so forth. Systematic risk can be calculated by multiplying the variance of the market with the beta. Beta is a measure of volatility of a security or portfolio return to the market return. Unsystematic risk is a risk that can be eliminated by diversification. This risk occurs in a particular company or industry due to the problem in their: structure of capital, asset structure, liquidity, yield and so forth.

Investors usually want to maximize their expected return with given risk when they invest in portfolio, this is called efficient portfolio. While optimal portfolio is a portfolio choose by the investors among alternatives of efficient portfolios ([8], 2001:74). Usually investors choose the portfolio that is in accordance with their preferences of risk and return. To calculate

To calculate exactly how much return that will be earned by an investment in the future is very difficult, it can only be estimated. An investment's return in the future is called expected return. The expected return of an investment can be very different with its realized return. Besides calculating his investment's return, an investor has to calculate the risk of his investment also. An investment's risk is a deviation between expected return and actual return ([8], 2001:51)

Single index model is a model develop by Sharpe, this method can be used to simplify the calculation in Markowitz method by using input parameter. Single index model can also use to calculate expected return and risk of portfolio ([5], 2003:231). Single index model assumed that stocks' return

have same reaction to one factor or single index included in the model. The sensitivity of stocks' return is calculated by beta ([3], 2005:82)

### RESEARCH METHOD

This study use quantitative method using time series quarterly data from 2010 to 2013. The analysis data in this study are as follows:

1. Stock's rate of return and risk.

Return is calculated by reducing closing price t period with t-1 period, add it with dividend paid then divided it with closing price t-1 period ([7] et.al, 2003:238)

$$R_i = \frac{(P_t - P_{t-1}) + D_t}{P_{t-1}} \quad (1)$$

where:

- $R_i$  = realized return
- $P_t$  = Price of stock period t
- $P_{t-1}$  = Price of stock period t-1
- $D_t$  = dividendat period t

Expected return is calculated using the following formula ([9], 2011:5):

$$E(R_i) = \sum_{t=1}^n \frac{R_{it}}{n} \quad (2)$$

Where:

- $E(R_i)$  = expected return of stock<sub>i</sub>
- $R_{it}$  = return stock<sub>i</sub> at period t
- n = period

$$\sigma_i^2 = \sum_{t=1}^n \frac{[R_{it} - E(R_i)]^2}{n} \quad (3)$$

Where :

- $\sigma_i^2$  = varians return stock i
- $R_{it}$  = returnstock i at period t
- $E(R_i)$  = expected return stock i
- n = period of observation

2. The te Market rate of return and risk Tingkat *return* dan risiko pasar

Market rate of return

Market rate of return is calculated from return of the composite index (IHSG) ([5], 2003:232):

$$R_{m,t} = \frac{IHS G_t - IHS G_{t-1}}{IHS G_{t-1}} \quad (4)$$

Where:

$R_m$  = market return return at period t

$IHS G_t$  = composite index at period t

$IHS G_{t-1}$  = composite index at period t-1

Market expected rate of return is calculated:

$$E(R_m) = \frac{\sum_1^n R_m}{n} \quad (5)$$

where:

$E(R_m)$  = market expected rate of return

$R_m$  = market rate of return

n = period

Market risk is the difference between market's expected return and its realized return, can be calculated by the formula:

$$\sigma_m^2 = \sum_{t=1}^n \frac{[R_{mt} - E(R_m)]^2}{n} \quad (6)$$

where:

$\sigma_m^2$  = variance market return

$E(R_m)$  = market expected return

$R_{mt}$  = market return period t

n = period

### 3. Beta and Alpha

Beta is a coefficient that measures the effect of changes in the market returns to changes in stock returns. Beta can be calculated by first calculating the covariance between stock returns and market return. Covariance between the stock return and the market return can be calculated by ([6], 2010:176):

$$\sigma_{im} = \sum_{t=1}^n [R_i - E(R_i)][R_m - E(R_m)] \quad (7)$$

where:

$\sigma_{im}$  = the covariance between security and market

$R_i$  = one possible return on security

$E(R_i)$  = the expected value of the return on security

n = the number of likely outcomes for a security for the period

next Beta is calculated by ([1] et.al, 2002:302):

$$\beta_i = \frac{\sigma_{im}}{\sigma_m^2} \quad (8)$$

where:

$\beta_i$  = stock's beta

$\sigma_{im}$  = covarians return between stock<sub>i</sub> and market return

$\sigma_m^2$  = varians market return

Alpha is a variable that is not influenced by the market return. In other words, this variable is an independent variable, in contrast to the beta which is the dependent variable because it is affected by the market return, it can be calculated by ([1] et.al, 2002:295):

$$\alpha_i = E(R_i) - \beta_i \cdot E(R_m) \quad (9)$$

where :

$\alpha_i$  = alpha of a stock

$E(R_i)$  = the expected value of the return on security

$E(R_m)$  = expected market return

### 4. The Varians of residual error

The variance of the residual error is a variable that indicates the magnitude of the risk that is unique to the company, it can be calculated with ([1] et.al, 2002:295):

$$\sigma_{si}^2 = \sigma_i^2 - \beta_i^2 \cdot \sigma_m^2 \quad (10)$$

where:

$\sigma_{si}^2$  = variance of residual error

$\sigma_i^2$  = varians of stock<sub>i</sub>

$\beta_i^2$  = stock's beta

$\sigma_m^2$  = variance of market return

### 5. The Determining the Optimal Portfolio Using Single Index Model

After we calculate return, variance, beta, and alpha of each stock, the next step is to determine the optimal portfolio using a single index model by calculating the degree of Excess Return to Beta (ERB) and determines Cut off Rate (Ci), as follows:

Excess Return to Beta level (ERB) is the difference between the expected return and the market return divided by beta. ERB describes the relation of return per-unit risk of a security. ERB can be calculated by ([5], 2003:253):

$$ERBi = \frac{E(Ri) - Rrf}{\beta_i} \quad (11)$$

where :

ERBi = excess return to beta of stock<sub>i</sub>

E(Ri) = expected return of stock<sub>i</sub>

Rbr = risk free rate of return

$\beta_i$  = Beta<sub>i</sub>

Cut off Rate (Ci) is a cut-off point used to determine whether a stock can be included into a portfolio or not. Shares that are chosen to be included in the portfolio are stocks that have Ci ≤ ERB. Cifor each of the securities is calculated by ([2], 2001:194):

$$C_i = \frac{\sigma_m^2 \sum [E(R_i) - R_{br}] \cdot \beta_i}{1 + \sigma_m^2 \sum \frac{\beta_i^2}{\sigma_{\epsilon i}^2}} \quad (12)$$

where:

E(Ri) = expected return of stock<sub>i</sub>

Rbr = risk free rate of return

$\beta_i$  = Beta<sub>i</sub>

$\sigma_m^2$  = variance of market return

$\sigma_{\epsilon i}^2$  = variance of residual error

## II. USING THE TEMPLATE

### 6. Afte Determine Proportion of fund Invested in Portfolio (Wi)

Once the portfolio is formed, then we can determine the proportion of funds (Wi) of each stock, Wi can be calculated by:

$$W_i = \frac{X_i}{\sum_{j=1}^k X_j} \quad (13)$$

With Xi :

$$X_i = \frac{\beta_i}{\sigma_{\epsilon i}^2} (ERBi - C^*) \quad (14)$$

where:

Wi = proportion of stock<sub>i</sub>

k = number of stocks in the optimal portfolio

$\beta_i$  = Beta<sub>i</sub>

$\sigma_{\epsilon i}^2$  = variance of residual error

ERBi = excess return to beta of stock<sub>i</sub>

C\* = cut-off point (which is the largest value)

### 7. The temp Calculate Return and Risk of Portfolio

Expected return of a portfolio is a weighted average of the returns of the individual stock in the portfolio, it can be calculated by

$$E(R_p) = \alpha_p + \beta_p \cdot E(R_m) \quad (15)$$

where:

E(R<sub>p</sub>) = expected return of portfolio

$\alpha_p$  = weighted average of each stock's alpha

$\beta_p$  = weighted average of each stock's beta

E(R<sub>m</sub>) = expected market return

Portfolio risk can be calculated by determining the magnitude of the variance of the portfolio. Portfolio variance can be calculated by:

$$\sigma_p^2 = \beta_p^2 \cdot \sigma_m^2 + \sum_{i=1}^n W_i^2 \cdot \sigma_{\epsilon i}^2 \quad (16)$$

where:

$\sigma_p^2$  = variance of portfolio

$\beta_p^2 \cdot \sigma_m^2$  = risks that related to market

$W_i^2 \cdot \sigma_{\epsilon i}^2$  = weighted average of each stock's risk

## RESULT OF THE STUDY

### Tabel 1 Number of Samples

The population in this research is all companies' stock listed in the Indonesia Stock Exchange during the period of 2010-2013. Based on predetermined criteria as sample, the number of samples in this study were 28 companies. Two companies do not meet the criteria listed in the sample because they start listed in JII in 2012.

### Analysis of Market's return and Stock's return

Chart 1 illustrates comparison of mean return of IHSG and return of 28 stocks listed in the Jakarta Islamic Index during 2010-2013. Chart 1 illustrates comparison of mean return of IHSG and return of 28 stocks listed in the Jakarta Islamic Index during 2010-2013.



$\beta < 1$		$\beta > 1$						NO	CODE	EXPECTED RETURN OF STOCK	VARIANCE $\sigma_i^2$	BETA $\beta_i$	SYSTEMATIC RISK $\sigma_m^2$	UNSYSTEMATIC RISK $\sigma_{ei}^2$	ERB	Ci	Wi
AA	EN	A	CP	IN	LP	PG											
LI	RG	KRA	IN	DY	KR	AS	1,3	AALI	0,00191	0,01649	0,67145	0,00288	0,01361	0,02642	0,00461		
0,6	0,9	1,7	2,8	1,4	1,1	1,3	1	ADRO	0,02696	0,02813	0,85905	0,00471	0,02342	0,04981	0,00834		
7145	8114	0914	4146	4108	8588	0772	2	AKRA	0,10924	0,05068	1,70914	0,01864	0,03204	0,05465	0,02010	0,15398	
							3	ANTM	0,11131	0,03504	0,73255	0,00342	0,03161	0,03706	0,00362		
							5	ASRI	0,15784	0,08057	2,13224	0,02902	0,05156	0,06660	0,02398	0,16587	
							6	BKSL	0,09170	0,11653	0,39292	0,00099	0,11554	0,19308	0,00163		
							8	BSDE	0,05456	0,04709	1,63351	0,01703	0,03006	0,02371	0,00857		
							9	CPIN	0,13584	0,20681	2,84146	0,05153	0,15528	0,04223	0,01052	0,03143	
							10	ENRG	0,01872	0,07027	0,98114	0,00614	0,06413	0,03522	0,00308		
							11	EXCL	0,07686	0,05887	1,35830	0,01177	0,04710	0,04493	0,00899	0,05684	
							12	INCO	0,01592	0,03081	1,35287	0,01168	0,01913	0,02347	0,00890		
							13	INDF	0,05374	0,01510	1,09500	0,00766	0,00744	0,03462	0,01755	0,14721	
							14	INDY	0,04556	0,04752	1,44108	0,01325	0,03427	0,04260	0,01188		
							15	INTP	0,02711	0,01663	1,13137	0,00817	0,00847	0,00997	0,00490		
							16	ITMG	0,00368	0,01798	0,89701	0,00514	0,01284	0,02175	0,00621		
							17	JSMR	0,08270	0,02446	1,32078	0,01113	0,01333	0,05063	0,02304	0,24852	
							18	KLBF	0,05512	0,06947	1,36073	0,01182	0,05765	0,02887	0,00491	0,01086	
							19	LPKR	0,06455	0,02510	1,18588	0,00898	0,01613	0,04108	0,01469	0,11835	
							20	LSIP	0,05188	0,06941	1,49895	0,01434	0,05507	0,04517	0,00933		
							21	MAPI	0,24929	0,36379	4,90331	0,15344	0,21035	0,04761	0,02008	0,05184	
							22	MNCN	0,21958	0,10513	1,36098	0,01182	0,09330	0,14971	0,01683		
							23	PGAS	0,03223	0,02452	1,30772	0,01091	0,01360	0,01254	0,00558		
							24	PTBA	0,01177	0,02452	0,99603	0,00633	0,01819	0,02771	0,00716		
							25	SMGR	0,04830	0,02413	1,26013	0,01013	0,01399	0,02577	0,01082	0,01511	
							26	TLKM	0,03649	0,05567	1,55290	0,01539	0,04028	0,03369	0,00931		
							27	UNTR	0,01605	0,02373	1,06845	0,00729	0,01644	0,00020	0,00006		
							28	UNV	0,07910	0,02183	0,06039	0,00002	0,02180	1,04756	0,00112		

Cut Off Point (C*)		0	1
		0,02398	

Table 3

Variance, Beta, Systematic and Unsystematic Risk, ERB, Cut-off Rate, and Proportion of each stock in Optimal Portfolio Period 2010 – 2013

After comparing the values of the ER and  $C_i$ , there are 14 stocks that have  $C_i \leq ER$ . Four stocks out of those 14 stocks have negative proportion, so these four stocks will not be considered to be chosen. Those stocks are PT Bumi Serpong Damai Tbk, PT Indocement Tunggal Prakarsa

**Conclusions**

**Table 4**

**Alpha Portfolio, Beta Portfolio, Expected Return Portfolio, and Variance Portfolio Period 2010 – 2013**

NO	Companies' stock code	Wi	$\alpha$	$\beta$
1	JSMR	24,852%	0,03090	1,32078
2	ASRI	16,587%	0,07421	2,13224
3	AKRA	15,398%	0,04221	1,70914
4	INDF	14,721%	0,01079	1,09500
5	LPKR	11,835%	0,01804	1,18588
6	EXCL	5,684%	0,02358	1,35830
7	MAPI	5,184%	0,05697	4,90331
8	CPIN	3,143%	0,02438	2,84146
9	SMGR	1,511%	-0,00112	1,26013
10	KLBF	1,086%	0,00175	1,36073
TOTAL		100%	0,28170	19,16698

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$E(R_p)$ (Expected Return Portfolio)	<b>0,1033</b>
$\sigma_p^2$ (Risk of Portfolio)	<b>0,0007</b>
$\sigma_p$ (Standard Deviation Portfolio)	<b>0,0274</b>

Sumber : Data Diolah

Table 4 shows that a portfolio made up of 10 companies with the proportion of funds to be invested. Risk generated by the portfolio ends to be lower than the risk of individual stocks listed in the Jakarta Islamic Index. This is proved that there turn and risk of the stock would be optimal if one is making diversification and doing analysis to make optimal portfolio, rather than investing only in one company's stock, investing using random model and not doing any analysis at all.

**References**

[1] Bodie, Zvi, Alex, dan Alan, *Investment, Fifth Edition*, McGraw-Hill, Inc, New York. 2002.

[2] Hadiano, M. Sopian dan M. Fakhruddin . *Perangkat dan Model Analisis Investasi di Pasar Modal*, Buku Satu, Elex Media Komputindo, Jakarta. 2001.

[3] Halim, Abdul. *Analisis Investasi*, Edisi Kedua, Salemba Empat, Jakarta. 2005.

[4] \_\_\_\_\_ . *Dasar-dasar Teori Portofolio dan Analisis Sekuritas*, Edisi Keempat, Unit Penerbit dan Percetakan AMP YKPN, Yogyakarta. 2005.

[5] Jogiyanto, *Teori-teori Portofolio dan Analisis Investasi*, Edisi Ketiga, BPFE, Yogyakarta. 2003.

[6] Jones, Charles P. *Investments Principles and Concepts, Eleventh Edition*, John Wiley and Sons, Inc, New York. 2010.

[7] Ross, S.A., Westerfield, dan Jaffe. *Corporate Finance, Sixth Edition*, Mc Graw-Hill, Inc, USA. 2003.

[8] Tandililin, Eduardus, *Analisis Investasi dan Manajemen Portofolio*, Edisi Pertama, Kanisius, Yogyakarta. 2010.

[9] Zubir, Zalmi. *Manajemen Portofolio: Penerapannya Dalam Investasi Saham*, Salemba Empat, Jakarta. 2011.