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Lailany Yahya2 1,2 Department of Mathematics, Universitas Negeri Gorontalo Jl. Prof. Dr.
Ing. BJ. Habibie, Tilongkabila, Bone Bolango, Gorontalo, Indonesia Email:
resmawan@ung.ac.id, lailany.math@gmail.com ABSTRACT The study was aimed to
introduce a new model construction regarding the transmission of Coronavirus Disease
(henceforth, COVID-19) in human population.

The mathematical model was constructed **by taking into consideration** several
epidemiology parameters that are closely identical with the real condition. The study
further conducted an analysis on the model by identifying the endemicity parameters of
COVID-19, i.e., the presence of disease-free equilibrium (DFE) point and basic
reproduction number.

The next step was to carry out sensitivity analysis to revealed that the parameters **????** ,
?? , , and **??** in sequence showed the most dominant sensitivity index towards **the basic**
reproduction number. Moreover, the results indicated positive index in parameters **??**
and **??** **????** that represented transmission chances during contact as well as contact rate
between vulnerable individuals and exposed individual. This suggests **that an increase in**
the previous parameter value could potentially enlarge the endemicity of COVID-19.

On the other hand, parameters **??** and , representing movement rate of **exposed**
individuals to the quarantine class and proportion of quarantined exposed individuals,
showed negative index. The numbers indicate **that an increase in the parameter value**
could decrease the -19 should focus on restriction of interaction between individuals
and optimization of quarantine.

Keywords: Sensitivity Analysis; Mathematical Model; Coronavirus Disease; COVID-19; Basic Reproduction Number INTRODUCTION Coronavirus Disease (henceforth, COVID-19) has shocked many thanks to its very rapid spread. Firstly identified to occur in Wuhan city of China, the disease has shortly become one of the main talking points as it reached the whole world and took thousands of death toll in a very short period.

The disease somewhat instigates all parties to conduct active measures in finding options to the best treatments and anticipatory means to prevent damage on a much wider scale. In mathematical perspective, the concern is closely related to implementation of mathematical model to identify potential solutions. Mathematical modelling is one of the key tools in epidemic preparation, including the COVID-19 pandemic.

The system allows one to comprehend and identify the correlation between COVID-19 spread and several epidemiology parameters, conduct preparatory Sensitivity Analysis of Mathematical Model of Coronavirus Disease (COVID-19) Transmission Resmawan 2 measures for future planning, and implement best practices of pandemic treatment. Previous studies, albeit little in number, has begun to address this problem and design mathematical model for COVID-19 transmission [1][2][3][4].

The model involved accurate and effective public health interventions. On top of that, a study compared between the outbreaks of current COVID-19 and previous MERS disease that spread in Middle Eastern countries and Korea [5]. Other studies designed mathematical model that predict COVID-19 cases in different countries [6][7].

Several models proposed in previous studies has discussed that the virus started from an unknown source and eventually began to spread to human population. The virus source, further referred to as reservoir variable, is suspected to be the place of first infection-to-human case. The present study introduces a different approach on mathematical modelling to the virus transmission by also involving the epidemiology parameters; a variable that is not discussed in previous studies.

Previous models have assumed that the virus transmission only occurs in interactions between individuals that have contracted the virus; differing from that, this article takes into consideration transmission cases caused by vulnerable individuals and exposed individuals. It views the importance of involving such parameters, considering the number of infections that occurred in the interaction between exposed individuals yet to be detected as infected.

Moreover, the model lays its emphasis on the pattern of transmission between human after the virus has become epidemic or pandemic, therefore, disregarding the reservoir variable. The model thus overlooks the process of first human infection and focuses on how the virus has spread within human-to-human interactions. In addition to that, the model employs new parameter representing death cases of COVID-19, pertaining to the fact that the virus has taken numbers of death toll.

The **model also takes into account** cases of quarantined individuals that were identified to be exposed to the virus. The following section elaborates construction of mathematical model in this study. Further, the article presents the research results in the form of model analysis. Within this section, **the study focuses on the** construction of basic reproduction number and sensitivity analysis to identify which parameter is the most sensitive to the change in basic reproduction number value. Finally, the last section proposes several conclusions to the research findings and discussion.

METHODS In this model, the total of human population was denoted in and **divided into six classes:** vulnerable individuals, exposed individuals in incubation period, infected individuals without clinical symptoms, infected individuals with clinical symptoms, quarantined individuals, and individuals that have recovered from COVID-19 (S, E, I_1, I_2, Q, R) . Therefore, the total population was stated in $N = S + E + I_1 + I_2 + Q + R$.

Recruitment rate of natural human natality and mortality is given the parameter λ and μ sequentially. Vulnerable individuals (S) will be infected from enough contact with other vulnerable individuals (S) , infected individuals with clinical symptoms (I_2) , and infected individuals without clinical symptoms (I_1) in respective rate of $\beta_1 S^2$, $\beta_2 S I_2$, and $\beta_3 S I_1$, in which is the infection probability during contact between individuals. $\beta_1, \beta_2, \beta_3$, and β_4 each states the contact rate between vulnerable individuals (S) and individual groups of S, I_1 , and I_2 .

The parameter β_1 and β_2 in respective order is the proportion of infected individuals without clinical symptoms and quarantined exposed individuals, while parameter β_3 states movement rate of **exposed individuals to the quarantined** individuals. Sensitivity Analysis of Mathematical Model of Coronavirus Disease (COVID-19) Transmission Resmawan 3 Parameter β_1 and β_2 each represent transmission rate after incubation period and status change to S and E class.

Quarantined individuals can be transferred to the class of infected individuals with symptoms **at the rate of** γ and proportion of ρ . Parameter γ, ρ, δ each states the recovery rate of infected individuals without symptoms, quarantined individuals, and

infected individuals with symptoms to be transferred to recovered individuals class ?? . Further, death **rate of COVID-19 in** ?? class is represented in ?? .

Schematically, the **transmission pattern of COVID-19** is displayed in Figure 1 below. Figure 1. Compartment diagram of COVID-19 transmission Based on the schematic diagram of virus transmission in Figure 6, the article presents model in the form of differential equation system as follows: $\frac{dS}{dt} = \lambda - \beta \frac{I}{N} S - (\mu + \delta) S$, $\frac{dE}{dt} = \beta \frac{I}{N} S - (\mu + \delta) E$, $\frac{dI}{dt} = \mu E - (\mu + \delta) I$, $\frac{dR}{dt} = (\mu + \delta) I - (\mu + \delta) R$, $\frac{dD}{dt} = \delta I - \delta D$ with early condition: $S(0) = S_0, E(0) = E_0, I(0) = I_0, R(0) = R_0, D(0) = D_0$. Dynamics of population in total is acquired by totaling the five equations in model (1), resulting in: $\frac{dN}{dt} = \lambda - (\mu + \delta) N$ (1) Sensitivity Analysis of Mathematical Model of Coronavirus Disease (COVID-19) Transmission Resmawan 4 $\mathcal{R}_0 = \frac{\beta I_0}{(\mu + \delta)}$ Positive invariant region that meets the model (1) is given by RESULTS AND DISCUSSION The Disease-free Equilibrium Point and **The Basic Reproductive Number** The equilibrium point is acquired at, therefore, the system of equation (1) indicates that the DFE point denoted by $(S^*, E^*, I^*, R^*, D^*)$, i.e., **The basic reproductive number** denoted by \mathcal{R}_0 is the expected value of infection rate per time unit.

The **infection occurs in a** vulnerable population, caused by an infected individual. Based on the equation system (1), the article generates equation that involves the classes of exposed population, infected population without symptom, and infected population with symptom, as follows: $\frac{dE}{dt} = \beta \frac{I}{N} S - (\mu + \delta) E$, $\frac{dI}{dt} = \mu E - (\mu + \delta) I$, $\frac{dR}{dt} = (\mu + \delta) I - (\mu + \delta) R$ (Further, **the basic reproduction number is** calculated by referring to the job [8].

From the equation (6), the study generates matrix and J , i.e. $J = \begin{pmatrix} -(\mu + \delta) & 0 & 0 & 0 & 0 \\ \beta \frac{I}{N} & -(\mu + \delta) & 0 & 0 & 0 \\ 0 & \mu & -(\mu + \delta) & 0 & 0 \\ 0 & 0 & 0 & -(\mu + \delta) & 0 \\ 0 & 0 & 0 & 0 & -\delta \end{pmatrix}$ Using the DFE point in equation (5), **Jacobian matrix and is** generated, i.e.

(4) (5) (2) (3) (6) (8) (7) Sensitivity Analysis of Mathematical Model of Coronavirus Disease (COVID-19) Transmission Resmawan 5 $\mathcal{R}_0 = \frac{\beta I_0}{(\mu + \delta)}$ **The basic reproduction number is** acquired from the largest positive eigenvalue of next generation matrix, G , i.e.

Therefore, it is generated that: $\mathcal{R}_0 = \frac{\beta I_0}{(\mu + \delta)}$ Further, can be stated in the form: with $\mathcal{R}_0 = \frac{\beta I_0}{(\mu + \delta)}$ $\mathcal{R}_0 > 1$ $\mathcal{R}_0 < 1$ $\mathcal{R}_0 = 1$

Baseline Parameter Values
 Parameter value implemented in the equation model (1) involves parameter value as a result of fitting process from several valid references based on real cases of COVID-19 that has been reported and published.

The complete parameter values implemented in the present study are displayed in the following Table 1. By referring to the parameter values in Table 1 in equation (10), the study acquires estimation of **basic reproduction number of 0.97**. This indicates that **every infected individual is** potential to infect minimum of three new individuals.

(9) (10) (11) Sensitivity Analysis of Mathematical Model of Coronavirus Disease (COVID-19) Transmission Resmawan 6 Table 1. Estimation of parameter values in COVID-19 cases

Parameter Description	Value	Source
Natural mortality rate	0.00048	[3]
Transmission probability during contact	0.1259	[4]
Rate of contact between vulnerable individual and exposed individuals	0.05	[2]
Rate of contact between vulnerable individual and infected individuals without clinical symptom	0.854302	[2]
Rate of contact between vulnerable individual and infected individuals with clinical symptom	0.11624	[3]
Proportion of infected individuals without clinical symptom	0.33029	[4]
Proportion of of quarantined exposed individuals	0.07	[3]
Movement rate of exposed individuals to quarantined individuals	0.04	[4]
Transmission rate after incubation period and transferred to infected with clinical symptom class	0.09	[2]
Transmission rate after incubation period and transferred to infected without clinical symptom class	0.05	[2]
Movement rate of quarantined individual to infected individuals with clinical symptoms	0.13266	[3]
Proportion of quarantined infected individuals with clinical symptoms	0.005	[4]
Recovery rate of infected individuals without clinical symptoms and transferred to R class	0.57	[2]
Recovery rate of quarantined individuals and transferred to R class	0.00048	[3]
Recovery rate of infected individuals with clinical symptoms and transferred to R class	0.00048	[4]
Mortality rate due to COVID-19	0.00048	[3]

78×10^{-5} Estimation Estimation Estimation Estimation [4] Estimation Estimation [3] [4] [4] [3] Estimation [4] [2] [2] [3] Sensivity Analysis To determine the most optimum approach in suppressing the number of infected individuals, one needs to identify several factors that contribute to the transmission of the virus and its prevalence. The first case of COVID-19 transmission closely relates to β_0 and persons exposed to COVID-19, as of β_1 , β_2 , β_3 , and β_4 group.

In this section, the study calculates the sensitivity index of each parameter model that correlates with the basic reproduction numbers, β_0 . This index provides information about the importance of each parameter to the model representing the transmission of COVID-19. The index is **used to identify the** parameter that has the most significant

impact on R_0 which is later served as the intervention target.

The parameter with a high impact in shows that the parameter has a dominant influence on the endemicity of COVID-19. The parameter of the sensitivity index towards **the basic reproduction number** is calculated using the approach similar to the one seen in [9]. Based on the explicit form of Sensitivity Analysis of Mathematical Model of Coronavirus Disease (COVID-19) Transmission Resmawan 7 R_0 in equation (10), the study derive the **analytic expression for the** sensitivity R_0 to the parameter β that is $\frac{\partial R_0}{\partial \beta} = \dots$ Table 2.

Model parameter index that is related to basic reproduction number

Parameter	Description	Sensitivity Index
β	Transmission probability during contact	Rate of contact between vulnerable individual and exposed individuals
μ	Movement rate of exposed individuals to quarantined individuals	Proportion of quarantined exposed individuals
β_1	Transmission rate after incubation period and transferred to infected with clinical symptom class	Transmission rate after incubation period and transferred to infected with clinical symptom class
β_2	Transmission rate after incubation period and transferred to infected without clinical symptom class	Transmission rate after incubation period and transferred to infected without clinical symptom class
μ_1	Natural mortality rate	Rate of contact between vulnerable individual and infected individuals with clinical symptom
μ_2	Recovery rate of infected individuals with clinical symptoms and transferred to R class	Proportion of quarantined infected individuals with clinical symptoms
μ_3	Movement rate of quarantined individual to infected individuals with clinical symptoms	Recovery rate of quarantined individuals and transferred to R class
μ_4	Proportion of infected individuals without clinical symptom	Rate of contact between vulnerable individual and infected individuals without clinical symptom
μ_5	Recovery rate of infected individuals without clinical symptoms and transferred to R class	Mortality rate due to COVID-19 in class of infected individuals without clinical symptoms

$+ 1.000 + 0.999 - 0.911 - 0.908 - 0.0715 - 0.0098 - 0.0061 + 0.0012 - 0.0011 + 0.0005 + 0.0005 - 0.0005 + 0.0004 + 0.00005 - 0.00005 - 6.4 \times 10^{-8}$

By referring to the formulation of equation (12) and parameter value in Table 1, it is generated the sensitivity index of each parameter in **the basic reproduction number** R_0 , **presented in Table 2.**

As an example, the sensitivity index of towards parameter β is $\frac{\partial R_0}{\partial \beta} = \dots$ (12) Sensitivity Analysis of Mathematical Model of Coronavirus Disease (COVID-19) Transmission Resmawan 8 = \dots (12) The sensitivity index in Table 2 sequentially shows the parameter with the highest sensitivity to the lowest sensitivity. In general, four parameters are significant to the changes in **the basic reproduction number.**

Those parameters include the chances of transmission during contact (β), the rate of contact between vulnerable individuals and exposed individuals (λ), the movement rate of individuals to the quarantine class (μ), and the proportion of quarantined exposed individuals (ρ). The parameter β and λ has a positive sensitivity index, while the parameter μ and ρ have a negative sensitivity index.

Parameters with a positive sensitivity index represent the positive significance in the increase of basic reproduction numbers. Thereby, enlarging (or scaling down) the value of β , while other parameter values same, will use the increase (or decline) in the basic reproduction numbers. Parameters with a negative sensitivity index represent the negative significance to the increase of basic reproduction numbers.

In other words, enlarging (or scaling down) the value of the parameter, while the other parameters remain the same, will contribute to the decline (or increase) in the basic reproduction numbers. The sensitivity index shows that contact with exposed individuals and the chance of transmission during the contact is the most dominant parameters contributing to the COVID-19 transmission.

On the one hand, the proportion of quarantined exposed individuals is the parameter that suppresses the transmission of the disease the most. Since $\rho = 0.999$, enlarging (or scaling down) the parameter ρ by 10% will result in a decline of the value ρ by 9.99%. The result that $\rho = 0.911$ signifies that enlarging (or scaling down) the parameter ρ by 10% will lead to a decline (or increase) in the value of ρ by 9.11%.

Interrupting the rate of transmission with exposed individuals and maximizing quarantine for exposed individuals and suspects are crucial. However, inadequate knowledge and lack of medical kits to detect those who have been contacted with COVID-19 are now hindering the countermeasures for combating the disease. It can be said that there is no strong evidence to determine those who have been contacted with COVID-19 and those who are not carrying the virus.

Due to the situations, preventive measures, such as social and physical distancing, are still the only option to halt the transmission of COVID-19. CONCLUSIONS The index of the sensitivity parameter shows that the parameter β and λ that represents the chance of transmission during the contact and the rate of contact between the vulnerable individuals and exposed individuals have the most dominant sensitivity to raise the endemicity of COVID-19. On the other hand, μ and ρ , represent the movement rate of exposed individuals to the quarantine and the proportion of quarantined exposed individuals, are the ones that can decrease the endemicity of COVID-19 the most.

The effectiveness of the measurement against COVID-19, therefore, can be assured by suppressing the interaction rate between vulnerable individuals and exposed individuals and maximizing treatment in the quarantine for those who are infected with the disease. All these attempts can be optimized by adhering to the health Sensitivity Analysis of Mathematical Model of Coronavirus Disease (COVID-19) Transmission Resmawan 9 protocol, such as by keeping space between oneself and the other, or well-known as social or physical distancing.

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