

Adaptive Fuzzy Integral Sliding-Mode Regulator for Induction Motor Using Nonlinear Sliding Surface

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ABSTRACT

An adaptive fuzzy integral sliding-mode controller using nonlinear sliding surface is designed for the speed regulator of a field-oriented induction motor drive in this paper. Combining the conventional integral sliding surface with fractional-order integral, a nonlinear sliding surface is proposed for the integral sliding-mode speed control, which can overcome the windup problem and the convergence speed problem. An adaptive fuzzy control term is utilized to approximate the uncertainty. The stability of the controller is analyzed by Lyapunov stability theory. The effectiveness of the proposed speed regulator is demonstrated by the simulation results in comparison with the conventional integral sliding-mode controller based on boundary layer.

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1. INTRODUCTION

Induction motor (IM) has been widely applied in the industrial field owing to its less-maintenance, lower-cost and excellent-reliability. High variable speed performance of induction motor is achieved through field-oriented control (FOC). In field-oriented control (or vector control), the induction motor can be controlled in a manner similar to the control of separately excited DC motor. The major problem of FOC is the sensitivity to large uncertainties which are due to magnetization saturation, temperature variation, load disturbances, etc [1]. In order to improve the performance of speed regulator under uncertainties in mechanical parameters and load torque, many improved speed regulator of FOC were proposed for induction motor drives [1]-[4]. Due to the good robustness, fast dynamics response and easy implementation, the sliding-mode control has been used in the control of induction motor [5]-[7]. But sliding-mode control is suffering from the chattering phenomenon. One effective solution is replacing the sign function by continuous saturation functions [8]. Boundary layer is a popular saturation function at the cost of the increased steady-state tracking error. The investigations on integral sliding-mode controller for induction motor can be found in [9]-[11]. In [9], an integral sliding-mode control strategy using saturation function was used to stabilize speed tracking of each induction motor while synchronizing its speed with the speed of other motors. A sliding-mode controller was presented for sensorless FOC of induction motor with model reference adaptive system in [10], where an integral sliding-mode control using boundary layer was designed. An integral sliding-mode control using boundary layer was adopted for speed controller of induction motor drives with reference model and a Luenberger observer in [11].

However, the windup problem and the convergence speed problem are not discussed in the above integral sliding-mode control strategies for speed regulator of FOC. As mentioned in [12], the integral action may lead to windup problem, and significant overshoot may occur that requires long time for recovery. To

eliminate the windup phenomenon for an integral sliding-mode control, the integral action was turned on only when the norm of tracking errors was lower than a predetermined value in [12]. Moreover, it is well-known that the integral action may slow down the convergence speed of tracking error. The derivative action may speed up the convergence speed of tracking error, but as we know the time derivative of mechanical speed (accelerated mechanical speed) is sensitive to the noise and difficult to obtain at present even using improved differentiators such as nonlinear differentiator [13] and sliding mode differentiator [14]. Hence, accelerated mechanical speed is seldom employed in practical speed regulator of FOC. On the other hand, the investigation of fractional-order control has attracted more and more interests. The fractional-order controller is the extension of integer-order controller [15], which introduces extra degrees of freedom. The fractional-order sliding-mode control were discussed in [16] and [17]. A fractional-order integral sliding-mode flux observer was provided to estimate the d- and q-axis fluxes in the stationary reference frame for sensorless vector controlled induction motors in [16]. A fractional-order sliding-mode control scheme based on parameters auto-tuning for the velocity control of permanent magnet synchronous motor was proposed in [17].

The main contribution of this paper lies in the following three aspects: (1) An adaptive fuzzy sliding-mode controller is proposed and successfully applied to the speed regulator of induction motor. (2) Combining the conventional integral sliding surface with fractional-order integral, a nonlinear sliding surface is proposed for the integral sliding-mode speed regulator, which can overcome the windup phenomenon and speed up convergence. (3) The adaptive fuzzy control term based on the nonlinear sliding surface is applied to approximate the uncertainty.

2. DYNAMIC MODEL OF INDUCTION MOTOR

The mathematics model of an induction motor can be written in the rotor rotating reference frame (d-q) [10] as follows:

$$\begin{aligned}\frac{d\omega_r}{dt} &= \rho\psi i_q - \beta T_L - \alpha\omega_r \\ \frac{d\psi}{dt} &= -a\psi + aL_m i_d \\ \frac{di_q}{dt} &= -\delta i_q - v\omega_r\psi - \omega i_d + bu_q \\ \frac{di_d}{dt} &= -\delta i_d + v\omega_r\psi + \omega i_q + bu_d\end{aligned}\quad (1)$$

Where $\rho = n_p L_m / (J_m L_r)$, $a = R_r / L_r$, $b = 1 / (L_\sigma L_s)$, $\alpha = B_m / J_m$, $\beta = 1 / J_m$, $v = L_m / (L_\sigma L_s L_r)$, $\delta = (R_s L_r^2 + R_r L_m^2) / (L_\sigma L_s L_r^2)$; ω_r and ω are the rotor mechanical speed and the synchronous speed; ψ is the rotor flux; L_m is the mutual inductance; $L_\sigma = 1 - L_m^2 / (L_r L_s)$ is the motor leakage inductance; i_d and i_q are the d, q-axis stator currents; R_r and L_r are the rotor resistance and inductance; R_s and L_s are the stator resistance and inductance; n_p is the number of pole pairs; u_d and u_q are the d, q-axis stator voltages; T_L is the external load torque; J_m and B_m are the mechanical inertia of moment and the damping torque coefficient; electromagnetic torque of an induction motor is defined as:

$$T_e = n_p L_m \psi i_q / L_r \quad (2)$$

From (1) and (2), one has:

$$\frac{d\omega_r}{dt} = -\alpha\omega_r - h + \beta T_e \quad (3)$$

Where $h = T_L / J_m$. Consider the uncertainties in (3), one gets:

$$\frac{d\omega_r}{dt} = -(\alpha + \Delta\alpha)\omega_r - (h + \Delta h) + (\beta + \Delta\beta)T_e \quad (4)$$

$$u = \begin{cases} J_m[\zeta + u_f + fS + K\text{sat}(S/\varphi)] + (J_m - B_m)e & |e| \leq \gamma_1 \\ J_m[\zeta + u_f + fS + K\text{sat}(S/\varphi)] + J_m {}_0D_t^{\nu+1}e - B_me & \gamma_1 < |e| \leq \gamma_2 \\ -B_me + J_m\xi + J_mu_f + fJ_mS + KJ_m\text{sat}(S/\varphi) & |e| > \gamma_2 \end{cases} \quad (9)$$

Where u_f is the adaptive fuzzy control term to approximate the uncertainty term, $\text{sat}(\cdot)$ is the saturation function defined as:

$$\text{sat}(S/\varphi) = \begin{cases} S/\varphi & |S| \leq \varphi \\ \text{sgn}(S) & |S| > \varphi \end{cases} \quad (10)$$

Where $\text{sgn}(\cdot)$ is the sign function, φ is the width of boundary layer which can reduce the chattering phenomenon.

The fractional-order derivative control term $J_m {}_0D_t^{\nu+1}e$ in (9) is used to speed up convergence of speed tracking error. The approximation of fractional-order derivate and integral plays an important role in the fractional-order control. We adopt the integer-order model to approximate the fractional-order derivate and integral in a suitable frequency interval [18]. The fractional-order derivative used in the proposed controller is not sensitive to the noise beyond the selected frequency interval.

The fuzzy input variables of the adaptive fuzzy control term [19], [20] are S and e . By using the singleton fuzzification, product inference engine and center average defuzzification, the adaptive fuzzy control term is given as:

$$u_f = \mathbf{b}^T \mathbf{w} = \sum_{j=1}^m \frac{\prod_{i=1}^n \mu_{F_{ij}} \cdot \hat{u}_j}{\sum_{j=1}^m \prod_{i=1}^n \mu_{F_{ij}}} \quad (11)$$

Where $\mathbf{b} = [\hat{u}_1, \hat{u}_2, \dots, \hat{u}_m]^T$ is the consequent parameter vector, \mathbf{w} is the vector of fuzzy basis functions, $n = 2$, $\mu_{F_{ij}}$ are the membership functions of input variables, \hat{u}_j is the point in output space of the fuzzy system at which the membership function of output variable achieves its maximum value, m is the number of fuzzy rules.

The parameter vector is adapted according to the following updating law:

$$\frac{d\mathbf{b}}{dt} = \begin{cases} rS\mathbf{w} & ((\|\mathbf{b}\| < M_1) \text{ or } (\|\mathbf{b}\| = M_1 \text{ and } S\mathbf{b}^T \mathbf{w} \leq 0)) \\ 0 & \text{others} \end{cases} \quad (12)$$

Where r and M_1 are the positive design parameters.

4. STABILITY ANALYSIS

The optimal parameter vector is defined as:

$$\mathbf{b}_0 = \arg \min_{\mathbf{b} \in \Omega} [\sup_{\|\mathbf{x}\| \leq N_1} |\eta(\mathbf{x}) - u_f|] \quad (13)$$

And λ is defined as the minimal approximation error.

Choose the Lyapunov functions as:

$$V_1 = \frac{1}{2} S^2(t) \quad (14)$$

$$V_2 = \frac{1}{2} S^2(t) + \frac{1}{2r} \mathbf{q}^T(t) \mathbf{q}(t) \quad (15)$$

Where $\mathbf{q} = \mathbf{b} - \mathbf{b}_0$.

The derivative of Equation (14) with respect to time is:

$$\frac{dV_1}{dt} = S \frac{dS}{dt} = S(-fS - K_{\text{sat}}(S/\varphi) + \eta(t)) \quad (16)$$

If $|S| > \varphi$, then:

$$\frac{dV_1}{dt} = S(-fS - K_{\text{sat}}(S/\varphi) + \eta(t)) \leq -fS^2 - K|S| + |\eta(t)||S| \quad (17)$$

Thus, if the condition of $K \geq |\eta(t)|$ is satisfied, $\frac{dV_1}{dt} \leq 0$ holds, and $\frac{dV_1}{dt} = 0$ only when $S = 0$.

On the other hand, If $|S| \leq \varphi$, considering (13), the derivative of Equation (15) with respect to time is:

$$\frac{dV_2}{dt} = S \frac{dS}{dt} + \frac{1}{r} \mathbf{q}^T \frac{d\mathbf{b}}{dt} \quad (18)$$

From (10), (11), (12) and (18), then:

$$\frac{dV_2}{dt} = S \frac{dS}{dt} + \frac{1}{r} \mathbf{q}^T \frac{d\mathbf{b}}{dt} = S[-fS - K_{\text{sat}}(S/\varphi) + \lambda] = S[-fS - KS/\varphi + \lambda] \quad (19)$$

If the adaptive fuzzy control term is properly designed, λ is sufficiently small, then $\frac{dV_2}{dt} \leq 0$ holds, and $\frac{dV_2}{dt} = 0$ only when $S = 0$. That means Lyapunov function V_2 will decrease gradually and the sliding surface will converge to zero. If the system of sliding surface is stable, the speed tracking error will converge to zero.

5. SIMULATION RESULTS

Simulations are carried out using the Simulink package of MATLAB. The overall control structure for the simulation is shown in Figure 1. The specifications and nominal parameters of motor operated using direct rotor field orientation are given in Table 1 [1].

Table 1. Specifications and Nominal Parameters of an Induction Motor

Motor parameter	Value
Output power (HP)	50
Rated voltage (V)	460
Number of pole pairs (P)	2
Rated frequency (Hz)	60
Stator resistance (Ω)	0.087
Rotor resistance (Ω)	0.228
Stator inductance (mH)	35.5
Rotor inductance (mH)	35.5
Mutual inductance (mH)	34.7
Mechanical inertia of moment ($\text{kg}\cdot\text{m}^2$)	2
Damping torque coefficient ($\text{N}\cdot\text{m}\cdot\text{s}$)	0.2

The operating sequences are described as follows. The initial load torque is constant ($0\text{N}\cdot\text{m}$). After the initial constant speed reference of 90rad/s from time $t=0$ to 0.1s . From time $t=0.1$ to 0.25s , the speed reference is increased linearly from 90 to 120rad/s , and then from $t=0.6$ to 0.9s speed reference is decreased from 120 to 90rad/s . At time $t=1.1\text{s}$ constant load torque ($190\text{N}\cdot\text{m}$) is applied.

The values of mechanical inertia of moment J_m and damping torque coefficient B_m are $0.831\text{kg}\cdot\text{m}^2$ and $0.5\text{N}\cdot\text{m}\cdot\text{s}$ during the simulation, i.e., there are uncertainties in the mechanical parameters. Simulation tests have been performed in order to compare the dynamic performance of the proposed speed regulator with

the conventional integral sliding-mode controller based on boundary layer, i.e., the proposed controller without the nonlinear sliding surface of Equation (7) and the adaptive fuzzy control term of Equation (11).

In the frequency domain, the fractional-order derivative of ${}_0D_t^{\nu+1}e$ can be expressed as $s^{\nu+1}$, where s is the Laplace variable. Figure 2 and Figure 3 show the bode diagram of the fractional-order derivative $s^{0.2}$ in the simulation and the bode diagram of the integer-order derivative s .

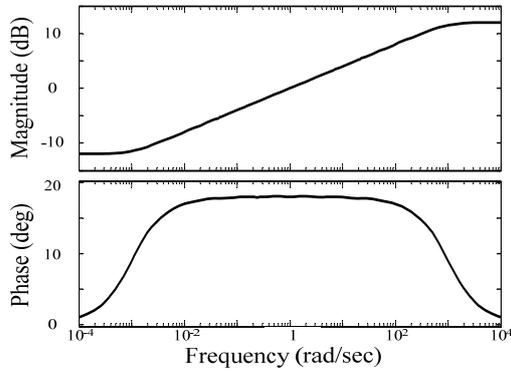


Figure 2. Bode diagram of $s^{0.2}$ in the simulation

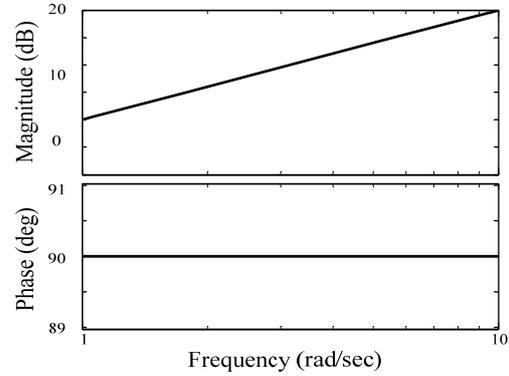


Figure 3. Bode diagram of s

The design parameters of the proposed speed regulator are $\nu = -0.8, \varphi = 1.5, \gamma_1 = 1, \gamma_2 = 5, r = 100, M_1 = 20, a_1 = 1, a_2 = 1, f = 1, K = 100$ and the fuzzy membership functions of e are designed as:

$$\begin{aligned} \mu_{F_{11}} &= \min(1, \max(0, 1 - (4e + 6)/3)); \mu_{F_{12}} = \max(0, \min(1 + (4e + 3)/3, 1 - (8e + 6)/3)); \\ \mu_{F_{13}} &= \max(0, \min(1 + (8e + 3)/3, 1 - (8e + 3)/3)); \mu_{F_{14}} = \max(0, \min(1 + 8e/3, 1 - 8e/3)); \\ \mu_{F_{15}} &= \max(0, \min(1 + (8e - 3)/3, 1 - (8e - 3)/3)); \mu_{F_{16}} = \max(0, \min(1 + (8e - 6)/3, 1 - (4e - 3)/3)); \\ \mu_{F_{17}} &= \min(1, \max(0, 1 + (4e - 6)/3)) \end{aligned}$$

The fuzzy membership functions of S are the same as those of e . The sliding surface of the compared controller is selected as $S = e + e_1$.

Figure 4 shows the desired motor speed (Dash-dot line), the rotor speed based on the compared controller (Dashed line) and the rotor speed based on the proposed controller (Solid line). It is clear that the rotor speed performance of the proposed controller is better than that of the compared controller after the step change of external load torque.

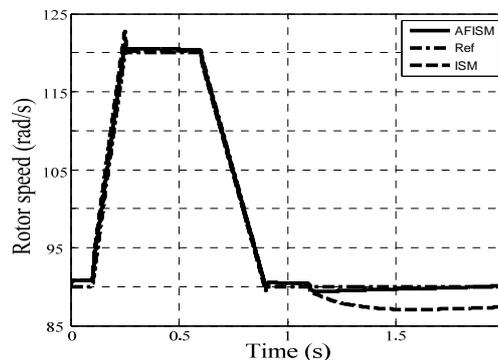


Figure 4. Reference speed and rotor speed response

The performances of the motor torque are illustrated by Figure 5 and Figure 6. It is seen that the motor torques are within reasonable ranges in Figure 5-6.

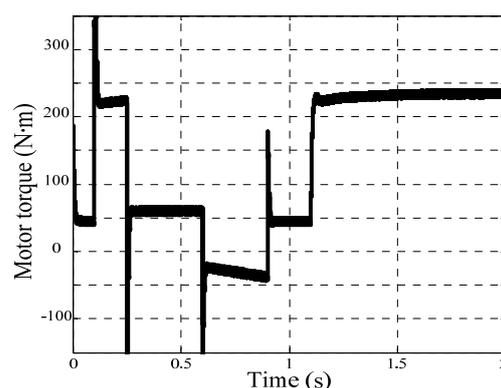
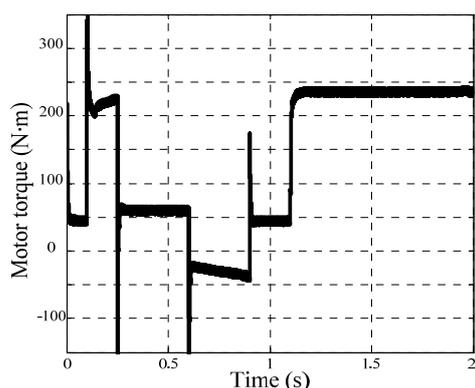


Figure 5. Torque response of the proposed controller Figure 6. Torque response of the compared controller

The simulation results reveal that the presented method has better tracking performance than the conventional integral sliding-mode controller based on boundary layer under uncertainties in the mechanical parameters and load torque.

6. CONCLUSION

In this paper, an adaptive fuzzy sliding-mode vector control has been presented for speed regulator of induction motor. It is proposed as a sliding-mode controller which has a nonlinear sliding surface to overcome the windup phenomenon of conventional integral sliding-mode speed controller strategy and speed up convergence by fractional-order derivative control term which is not sensitive to the noise beyond the selected frequency interval. Moreover, the proposed sliding-mode controller incorporates a fractional-order adaptive fuzzy control term based on the nonlinear sliding surface to approximate the uncertainty. Then the closed loop stability of the presented design has been proved by Lyapunov stability theory. Finally, by means of simulation examples, it has been shown that the proposed control method improves tracking performance of speed in comparison with the conventional integral sliding-mode controller based on boundary layer in presence of external load disturbance and mechanical parameter variations.

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