

# Correlation between Battery Voltage under Loaded Condition and Estimated State of Charge at Valve-Regulated Lead Acid Battery on Discharge Condition using Open Circuit Voltage Method

Ahmad Qurthobi , Anggita Bayu Krisna Pambudi , Dudi Darmawan , and Reza Fauzi Iskandar

Department of Engineering Physics, School of Electrical Engineering, Telkom University, Indonesia

---

---

## Article Info

### Article history:

Received November 24, 2017

Revised January 23, 2018

Accepted February 18, 2018

### Keyword:

Battery

State of Charge

Open Circuit Voltage

## ABSTRACT

One of the common methods that developed to predict state of charge is open circuit voltage (OCV) method. The problem which commonly occurs is to find the correction parameter between open circuit voltage and loaded voltage of the battery. In this research, correlation between state of charge measurement at loaded condition of a Panasonic LC-VA1212NA1, which is a valve-regulated lead acid (VRLA) battery, and open circuit voltage had been analyzed. Based on the results of research, correlation between battery's measured voltage under loaded condition and open circuit voltage could be approached by two linearization area. It caused by  $K_v$ 's values tend to increase when measured voltage under loaded condition  $V_M < 11.64$  volt. However,  $K_v$  values would be relatively stable for every  $V_M \geq 11.64$  volts. Therefore, estimated state of charge value, in respect to loaded battery voltage, would increase slower on  $V_M < 11.64$  volts and faster on other range.

Copyright © 2018 Insitute of Advanced Engineering and Science.

All rights reserved.

---

---

## Corresponding Author:

Ahmad Qurthobi

Department of Engineering Physics, School of Electrical Engineering, Telkom University

Jalan Telekomunikasi No 1 Terusan Buah Batu

+62-813-20262968

qurthobi@telkomuniversity.ac.id

---

---

## 1. INTRODUCTION

Lead acid battery is a type of dry elements. Its commonly used as energy backup storage for remote communities, telecommunication systems, or electric vehicles[1]-[4]. The problems which commonly occur on lead acid type batteries are overcharge and overdischarge. Both condition create temperature changes and physical deformation on the battery which affect on its performances. Therefore, it needs to analyzed battery's state of charge (SoC)[5]-[10].

State of charge (SoC) is a ratio between available and maximum electrical charge that stored in the battery[2],[11]. SoC is a non-dimentional unit and it could be expressed in percent or value between 0 and 1. SoC is an important parameter which not only to avoid harmful condition, such as overcharge and overdischarge, but also to expand the battery lifetime. One of the methods used to estimate state-of-charge is open circuit voltage (OCV). Statistically, correlation between state of charge and open circuit voltage could be represented as an linear equation. However, as loads attached to the battery, the loading effect would be occurred. It would create gap between measured voltage and open circuit voltage[12]. Therefore, correlation between open circuit voltage and loaded battery voltage which culminated on their correlation with state of charge should be determined.

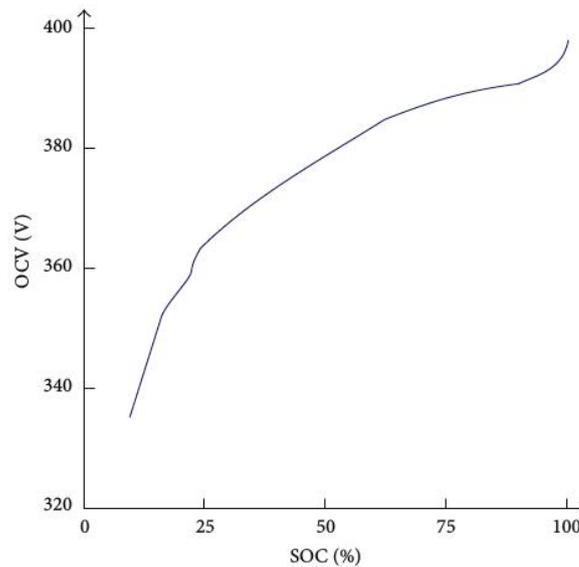


Figure 1. An example of typical correlation between state of charge and open circuit voltage[13]

In previous research, correlation between both variables in a Yuasa SWL2500 could be written as a constant value for several examination point[1]. Therefore, in this research, correlation between loaded battery voltage on discharge condition and open circuit voltage had been analyzed on a Panasonic LC-VA1212NA1, which is a valve-regulated lead acid (VRLA) battery. This research observes the changes of rest period parameter on the battery based on its loaded voltage at several points which leads to produce a precise estimation of state of charge.

## 2. RESEARCH METHOD

### 2.1. State of Charge and Open Circuit Voltage

As mentioned in section 1., state of charge or SoC is a non-dimensional unit which represents ratio between available and maximum charge stored in a battery. Hence, SoC is proportional to charge residues inside a battery and it could be represented as equation (1), where  $q_t$  and  $q_{max}$  represent, current and maximum charges values inside battery, respectively.

$$SOC_{\%} = \frac{q_t}{q_{max}} \times 100 \quad (1)$$

On the real condition, neither zero point of a battery equal to zero charge ( $q_0 \neq 0$ ) nor its maximum value equal to peak charge ( $q_{max} = q_{peak}$ ). The minimum and maximum charges values inside the battery are frequently mentioned by the manufacturers on battery's datasheet to keep its performances. Hence, equation (1) should be rewritten as equation (2), where  $q_{min}$  represents minimum charges value.

$$SOC_{\%} = \frac{q_t - q_{min}}{q_{max} - q_{min}} \times 100 \quad (2)$$

There are some methods developed for SoC estimation. One of those estimation methods is open circuit voltage (OCV)[1]. OCV method has been developed based on an assumption that a battery is equal to a capacitor and the amount of charges ( $q$ ) inside a capacitor is linearly proportional to its output voltage ( $V_t$ )(see equation (3)).

$$V_t = \frac{q_t}{C} \quad (3)$$

Statistically, if it is assumed that typical correlation between SoC and OCV is shown by figure 1, it could be approached by a linear formula such as equation (4)[13], where  $V_{min}$ ,  $\alpha_1$ , and  $\alpha_2$  are, respectively, battery's minimum voltage (recommended by manufacturer), a multiplier constant, and a correction factor.

$$SOC_{\%} = \alpha_1 \times (V_t - V_{min}) + \alpha_2 \quad (4)$$

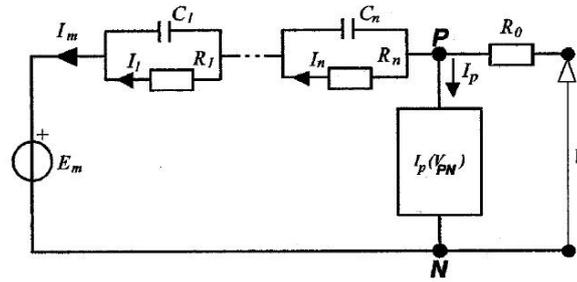


Figure 2. Lead acid equivalent network for both discharge and charge[12]

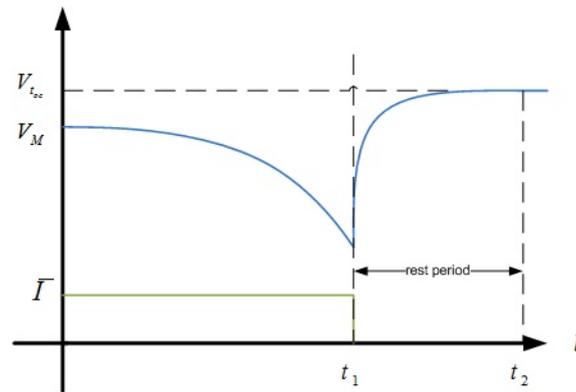


Figure 3. Typical voltage and current profile for a constant current discharge[12]

## 2.2. Battery Modelling and Rest Period

Equation (3) is only valid in specific conditions, such as when all of its loads are disconnected from the battery. However, removing loads from the battery for voltages examination creates a non-real time measurement. Barsali and Ceraolo(2002) define a lead acid battery's dynamic model to investigate its discharging dynamic behavior[12]. Lead acid equivalent network for charge and discharge are shown by figure (2). Furthermore, they also represent typical voltage and current profile for constant current discharge as shown on figure 3.

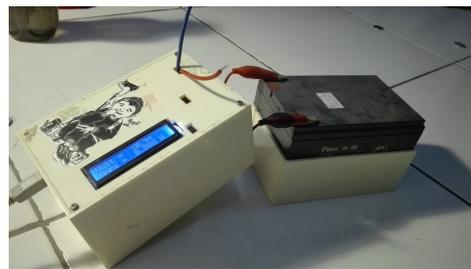
Figure 3 shows that there is exist a transition time required by the battery to show its open circuit voltage value after loads are removed. This transition time known as rest period [1],[2],[12]. Hence, OCV ( $V_{t_{oc}}$ ) of a battery could be written as equation (5)[1], where  $V_M$  is measured voltage when loads are attached to the battery and  $K_v$  is a parameter derived from  $V_{t_{oc}} - V_M$  after the battery is rested.

$$V_{t_{oc}} = V_M \pm K_v \quad (5)$$

## 2.3. Observing $K_v$

As mentioned in subsection 2.2.,  $K_v$  is a parameter derived from differences between open circuit voltage and loaded voltage. Its values could vary on every point. Therefore, it needs to observe  $K_v$  values at several points to determine its correlation with battery's voltage. To determine the value of  $K_v$  at some specified point, a testing had been done with the following steps:

1. As pre-conditioning process, a VRLA battery (Panasonic LC-VA1212NA1) has been charged until it reaches its maximum voltage value recommended by its manufacturer, in this case is 13 volt[14](Figure 4(a)).
2. Connect the battery with a 10 watt load and measure its terminal voltage (Figure 4(b)).



(a)



(b)

Figure 4. Battery charging and discharging process

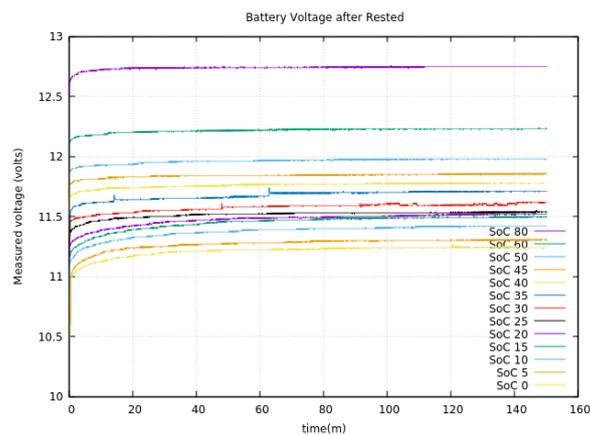


Figure 5. The changes of battery voltage measurement for 150 minutes

3. As soon when terminal voltage reach first point, remove load from battery and leave it rest for 150 minutes.
4. Monitor the change in battery voltage values, starting from the load released until the rest period ends.
5. Repeat step (2) to (4) for another monitoring point.

### 3. RESULT AND ANALYSIS

Figure 5 shows the change of experimental battery's voltage value when it rested for 150 minutes. This figure shows that loading effects which occurs on the battery results the measured voltage at loaded condition is lower than its open circuit voltage. The values are varies in range 0.22 - 0.74 volt.

Correlation between measured voltage under loaded condition  $V_M$  and open circuit voltage  $V_{oc}$  after rest period on the battery are shown in figure 6. It informs the gradient of correlation curve of  $V_M$  and  $V_{oc}$  for  $V_M \geq 11.64$  volt is relatively constant with  $\frac{\partial V_{oc}}{\partial V_M} \approx 1$  with small zero offset addition. However, for

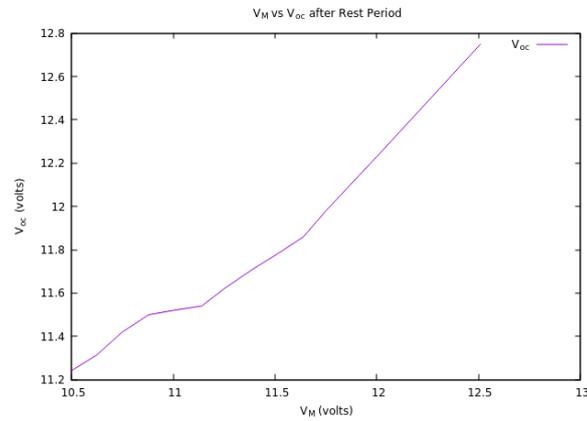


Figure 6. Correlation between measured voltage  $V_M$  under loaded condition and open circuit voltage  $V_{oc}$  after 150 minutes of rest period

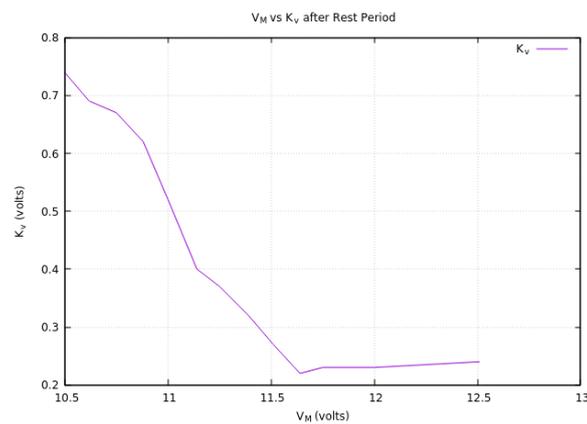


Figure 7. Correlation between measured voltage  $V_M$  under loaded condition and correction parameter  $K_v$

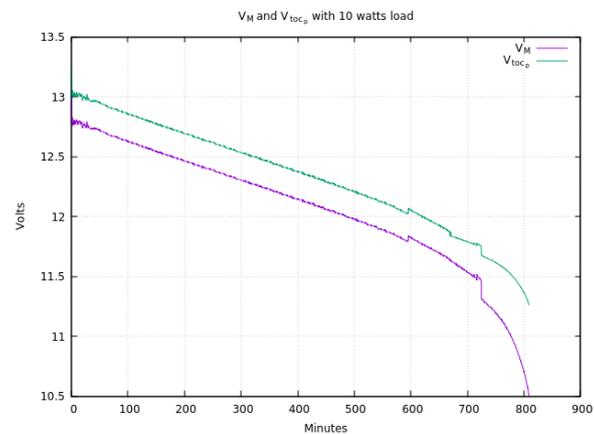


Figure 8. Measured voltage under loaded condition and estimated open circuit voltage in respect to time

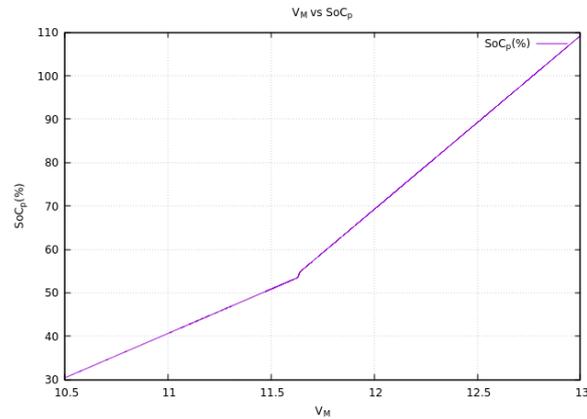


Figure 9. Correlation between  $V_M$  and  $\text{SOC}_p(\%)$

$V_M < 11.64$ , correlation between both variable relatively fluctuative and could be approached by equation (6).

$$V_{oc} = 0.50V_M + 6.02 \quad (6)$$

This condition yeilds correlation between  $K_v$  and  $V_M$  had negative gradient for every  $V_M < 11.64$  volts. In the other hand, it is relatively stable with average  $K_v = 0.23$  volt for  $V_M \geq 11.64$  volts (see figure 7). Hence, evolution ov  $K_v$  could be devided into two linearization condition and could be written as equation(7).

$$K_v = \begin{cases} -0.49V_M + 5.90; & \text{for } V_M < 11.64 \\ 0.23; & \text{for others} \end{cases} \quad (7)$$

However, the result shows different outcome with another research with another VRLA battery, where  $K_v$  values are almost constant for every inspection points(80%, 60%, 40%, and 20% of SoC) on Yuasa SWL2500 battery with 240 minutes of rest period[1].

Based on equation (5) and (7), correlation between measured loaded voltage and estimated open circuit voltage value in respect to time could be drawn as figure 8. As results of implementation of  $K_v$  values, the gap between both curves would increase as soon as measured voltage under loaded condition is less than 11.64 volts. Therefore, correlation between state of charge and  $V_M$  could be shown as figure 9 and could be written as equation (8).

$$\text{SoC}\% = \begin{cases} 20.44V_M - 184.64; & \text{for } V_M < 11.64 \\ 40V_M + 410.8; & \text{for others} \end{cases} \quad (8)$$

As validation process, testing on subsection 2.3. had been repeated with addition of new examination point at  $V_M = 12.24$  volts. Figure 10 shows correlation between estimated open circuit voltage  $V_{toc_p}$  and actual voltage  $V_{real}$ . This figure shows correlation between both variables could be approached with a linear formula and could be written as equation (9). It also informs the average absolute error between  $V_{toc_p}$  and  $V_{real}$  is 0.02 volt.

$$V_{real} = 1.02V_{toc_p} + 0.28 \quad (9)$$

#### 4. CONCLUSION

Based on the results of research, correlation between battery's measured voltage under loaded condition and open circuit voltage could be approached by two linearization area. It caused by  $K_v$ 's values tend to increase when measured voltage  $V_M < 11.64$  volt and correlation between both variables could be written as  $-0.49V_M + 5.90$  volt. However,  $K_v$  values would be relatively stable on 0.23 volt for every  $V_M \geq 11.64$  volts. Therefore, in respect to loaded battery voltage, estimated state of charge value would increase slower on  $V_M < 11.64$  volts and faster on other range. It shows different outcome with another research with another VRLA battery, where  $K_v$  values are almost constant for four inspection points(80%, 60%, 40%, and 20% of SoC) on Yuasa SWL2500 battery with 240 minutes of rest period.

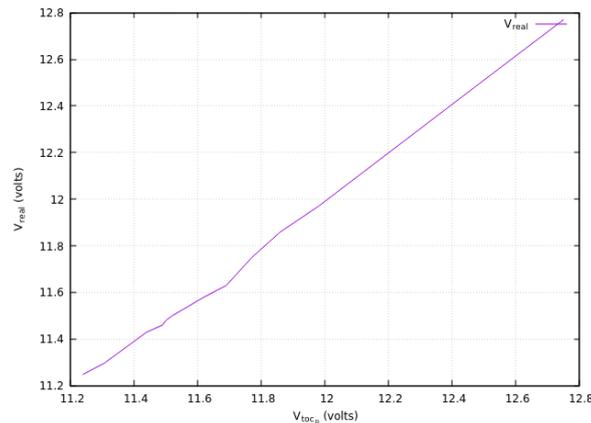


Figure 10. Correlation between  $V_{toc,p}$  and  $V_{real}$

## REFERENCES

- [1] A. Mariani, T. Stockley, K. Thanapalan, and J. Williams, Simple and Effective OCV Prediction Mechanism for VRLA Battery Systems, in The 3rd International Conference on Mechanical Engineering and Mechatronics, pp. 140(1)140(10), Aug. 2014.
- [2] S. Mischie and L. Toma, Behavior of the Lead Acid Battery after the Rest Period, WSEAS TRANSACTIONS on POWER SYSTEMS, vol. 3, pp. 111117, Mar. 2008.
- [3] K. Belmokhtar, H. Ibrahim, Z. Fger, and M. Ghandour, Charge Equalization Systems for Serial Valve Regulated Lead-Acid (VRLA) Connected Batteries in Hybrid Power Systems Applications, in International Renewable Energy Storage Conference, no. 99, pp. 277284, Mar. 2016.
- [4] A. Selmani, A. Ed-Dahhak, M. Outanoute, A. Lachhab, M. Guerbaoui, and B. Bouchikhi, Performance Evaluation of Modelling and Simulation of Lead Acid Batteries for Photovoltaic Applications, International Journal of Power Electronics and Drive System, vol. 7, pp. 472480, June 2016.
- [5] C. Unterrieder, C. Zhang, M. Lunglmayr, R. Priewasser, S. Marsili, and M. Huemer, Battery state-of-charge estimation using approximate least squares, Journal of Power Sources, pp. 274286, 2015.
- [6] S. Xie, R. Xiong, Y. Zhang, and H. He, The Estimation of State of Charge for Power Battery Packs used in Hybrid Electric Vehicle, in The 8th International Conference on Applied Energy , pp. 2678 2683, 2017.
- [7] V. Surendar, V. Mohakumar, S. Anand, Prasanna, and D. Vadana, Estimation of State of Charge of a Lead Acid Battery Using Support Vector Regression, in SMART GRID Technologies,, pp. 264 270, Aug. 2015.
- [8] Y. Wang, C. Zhang, and Z. Chen, State-of-charge estimation of lithium-ion batteries based on multiple filters method, in The 7th International Conference on Applied Energy, vol. 25, pp. 2635 2640, Elsevier, 2015.
- [9] X. Tang, B. Liu, and F. Gao, State of charge estimation of LiFePO4 battery based on a gain-classifier observer, in The 8th International Conference on Applied Energy, vol. 105, pp. 2071 2076, 2017.
- [10] S. Prasad and D. V. Kumar, Hybrid fuzzy charged system search algorithm based state estimation in distribution networks, Engineering Science and Technology, an International Journal, vol. 20, pp. 922933, 2017.
- [11] T. Wu, L. Liu, Q. Xiao, Q. Cao, and X. Wang, Research on SOC Estimation Based on Second-order RC Model, TELKOMNIKA, vol. 10, pp. 16671672, Nov. 2012.
- [12] S. Barsali and M. Ceraolo, Dynamical Models of Lead-Acid Batteries: Implementation Issues, IEEE TRANSACTIONS ON ENERGY CONVERSION, vol. 17, pp. 1623, Mar. 2002.
- [13] W. Y. Chang, The State of Charge Estimating Methods for Battery: A Review, ISRN Applied Mathematics, vol. 2013, no. 953792, pp. 17, 2013.
- [14] Panasonic, LC-VA1212. Panasonic Storage Battery, Co. Ltd.

**BIOGRAPHIES OF AUTHORS**

**Ahmad Qurthobi** is a lecturer and researcher at Department of Engineering Physics, School of Electrical Engineering, Telkom University (2013-present). He obtained Bachelor Degree in Telecommunication Engineering from STT Telkom (Indonesia) in 2007 and Master Degree in instrumentation and Control from Institut Teknologi Bandung (Indonesia) at 2011.

His researches are in fields of electric power, instrumentation, control system, renewable energy, and power electronics.

He is affiliated with PII as member.

For further info on his homepage: <http://qurthobi.staff.telkomuniversity.ac.id/>



**Anggita Bayu Kresna Pambudi** is an engineer of National Electric Company of Indonesia. He obtained Bachelor Degree in Engineering Physics from Telkom University (Indonesia) at 2016.

His researches are in fields of instrumentation, and measurement.

Beside his activity as engineer, he also runs a start up design company called Dodlezig.

For further info on his homepage: <http://www.anggitabay.com/>



**Dudi Darmawan** is a lecturer and researcher at Department of Engineering Physics, School of Electrical Engineering, Telkom University (1999-present). He obtained Bachelor Degree in Physics in 1998, Master Degree in instrumentation and Control at 2004, and Doctoral Degree in Engineering Physics at 2015 from Institut Teknologi Bandung(Indonesia).

His researches are in fields of non-destructive testing, instrumentation, tomography, and electromagnetics.

For further info on his homepage: <http://dudidw.staff.telkomuniversity.ac.id/>



**Reza Fauzi Iskandar** is a lecturer and researcher at Department of Engineering Physics, School of Electrical Engineering, Telkom University (2012-present). He obtained Bachelor Degree in Physics Education from Universitas Pendidikan Indonesia at 2003, and Master Degree in instrumentation and Control from Institut Teknologi Bandung (Indonesia) at 2011.

His researches are in fields of instrumentation, control system, power electronics, and renewable energy.

For further info on his homepage: <http://rezafauzii.staff.telkomuniversity.ac.id/>