182



A Model to Choose Hub and Route Determination

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ABSTRACT

Determining a transport hub is a strategic decision to build a good distribution flow. In this paper, We suggested a model for choosing hub locations as sources for companies. In previous studies, The determination of hub locations with a vehicle routing problem is not integrated. Therefore, this study built a model to assess the position of the hubs by considering the budget. The business should have a decision on vehicle routing with hubs to reduce total transport costs. In addition, the method of distribution of goods for hubs and non-hubs with third-party logistics was determined by the use of a vehicle routing problem. The optimal weight obtained through the analysis of sensitivity. In the sensitivity analysis, this study found that the best choice in this study was to use a weight of 0.9–1.0. It provides the lowest total cost of transport.



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1. Introduction

Based on a survey in 2016, Farber [1] found that online purchases have significantly increased. The business-to-consumer retail segment continues to grow on online shopping [2]. The growth of e-commerce provided the Logistics Company with an opportunity. The new logistics company does not usually have a large capital. The capital limitation makes it difficult to determine the hub that needs to be built. Hub is a special facility that functions as a point transfer facility [3]. Based on these benefits, the company has more power to develop their market to compete with other companies. There are several alternatives to consider in setting up hubs to avoid the wrong decision. It leads to an adverse impact on the company. Besides, the new logistics company does not know the route of the vehicle that must selected and passed to minimize the costs of logistics. The right decisions, a company, have the advantage of a hub building and minimizing the total transportation costs. The Vehicle Routing Problem (VRP) model was first introduced by Dantzig and Ramser [4]. Min [5] Developed multiple vehicle routing problems by considering pickup, delivery size, and traffic congestion. Baldacci, et









al. [6] and Domínguez-Martín, et al. [7] proposed routing for the heterogeneous fleet of the vehicle. El-Sherbeny [8] developed a model with a homogeneous product component. In the generalized vehicle routing problem (GVRP), the set of customers is divided into clusters and each cluster has a specific demand [9-14]. The objective is to a minimum cost set of delivery routes that serve the total demand of customers served by a single vehicle that does not exceed the capacity of the vehicle. The green vehicle routing problem (G-VRP) have proposed by Erdoğan and Miller-Hooks [15], Koç and Karaoglan [16], Montoya, et al. [17] and Andelmin and Bartolini [18] charging an EV was done in constant time. Another problem is that the charging time linearly depends on the state of the EV at its arrival [17, 19-22]. There is an E-VRP with Capacitated Charging Station by Froger, et al. [23].

In common, the companies manage the different hub assignment problems included selecting and allocating hubs. Companies assign nodes to transfer one of the hubs. In several studies, both location and allocation are known as NP-hard problems [24]. Regarding the determination of hubs, Klincewicz [25] was the first article to discuss the location hubs. The integration of operational, tactical, and strategic decisions require further elaboration [26-28]. Various criteria and aspects are the problems to improve. According to Weber [14], the concept of choosing a warehouse location for the first time by placing the warehouse is a way that the total distance traveled between the warehouse and the customer can be minimized. According to Vieira and Luna [27], different aspects can be considered during modeling as decision criteria or model restrictions. They consist of 1). Transportation; 2. Hub functionality; 3. Investment; 4. Offers and requests; 5. Markets; 6. Policy; and 7. Environment. Alumur, et al. [29], Campbell and O'Kelly [26] and Martí, et al. [30] used p-hub median and Farahani, et al. [31] used p-hub covering.

Although some research has been carried out on p-hub and VRP, no studies have been found which use 2-stage in this problem. The first stage was that the analysis process is carried out with criteria such as distance and weighted demand and investment in the form of limited capital. In the second stage, we analyzed the costs by implementing vehicle routing problems. This research aims to develop a mathematical model of the total cost of hubs and transportation by considering distance, demand, and investment and determining the route of the vehicle to minimize transportation costs. The innovation of this analysis is a model that combines the selection of hubs with the problems of vehicle routing. The model to be selected by a business is an ideal hub with capital constraints to achieve minimal transport costs. Organizations do have not only an optimum hub but also an optimum vehicle routing to reduce overall travel costs in order to make more profit. The remainder of the paper is structured as follows. The next section focuses on model development and data used. Section 3 provides the result and discussion along with the sensitivity analysis. Conclusions and directions for future research are assigned to the last section.

2. Methods

2.1. Assumptions

In this model, Determining the hub is a strategic decision that needs to be carefully considered. The company does not have a sufficient vehicle route to reduce transport costs. Several of the assumptions are used as follows: 1). Capacity meets the entire demand; 2). Vehicles have a uniform capacity, and 3). Alternatives to the hub location are available.



2.2. Model Development

In this research, there were some notations that researchers use. These notations are components of the model designed. Therefore, the model can run well. The notations are:

 c_{ij} : Transportation costs incurred when the vehicle moves from node i to node j

 x_{ijk} : Decision variables in VRP,

 $\mathbf{x}_{ijk} = \begin{cases} 1, \text{if vehicle k moves from node i to j} \\ 0, \text{otherwise} \end{cases}$

J_i : The distance between the hub

V : Number of vehicles

Y : Total Capital

N : Number of nodes (hub and non-hub)

q_i : Capacity of vehicle-i

d; : The demand of customer on hub-i

 I_i : Cost of making hub-i Ω : Weight distance

M : Capital budget or making hubs

H_i : Hub-i

L_i: The cost of 3rd party logistics when the hub is not built

a; : The weight value of hub-i

b_{ii} : Ranking value,

 $b_{ij} = \begin{cases} 1, \text{if weight value of hub} - i \ \geq \ \text{hub} - j \\ 0, \text{otherwise} \end{cases}$

P : Income / unit

E : Transportation cost / km

W_i: The capacity of 3rd party logistics-i

F_i: The decision variable on 3rd party logistics,

$$F_i = \begin{cases} 1, & \text{if a hub is built} \\ 0, & \text{if a hub is not built} \end{cases}$$

The first model is a model designed to maximize the use of capital to evaluate the center to be constructed. The decision process is based on the weight of the distance and the weight of the request. Therefore, each company can choose which weight is better suited to reduce the overall cost of transport. The first iteration is the following one.

$$\operatorname{Max} Y = \sum_{i=1}^{N} H_i \tag{1}$$

Subject to,

$$H_i = \sum_{\substack{i \neq j \\ j=1}}^{N} b_{ij} \tag{2}$$

$$b_{ij} = \begin{cases} 1, & a_i > a_j \\ 0, & a_i < a_j \end{cases}$$
 (3)

$$a_i = d_i (1 - \Omega) p - J_i \Omega E$$
(4)

$$\sum_{i=1}^{N} H_i I_i \le M ; \forall_i \in N$$
 (5)

$$\Omega \in (0,1) \tag{6}$$

Equation (2) is the cumulative number of ranking values for each hub after comparison of the weight values between hubs' made. Equation (3) is the process of assigning ranking values, which 1 if the weight of the ith-hub is greater than the value of the weight of the jth-hub and 0 otherwise. Equation (4) is an equation for calculating the weight for each prospective hub where each criterion has a weight. In this study, there are two weights used, Ω for distance and 1- Ω for request. Constraint (5) ensures that each hub to be built does not exceed the capital budget for the construction of a hub. Constraint (6) explains that Ω as a weight value between 0 and 1. After determining which hub to be built, the transportation costs will be calculated based on the predetermined hub(s) and non-hub(s).

The total transportation costs in the VRP are based on El-Sherbeny [8] with some modifications. The researchers added the cost of third party logistics when there are nonhubs in a company, and the company must deliver the goods. The total transportation cost model in the VRP is the following.

$$Min Z = \sum_{k=1}^{V} \sum_{i=1}^{N} \sum_{j=1}^{N} c_{ij} x_{ijk} + \sum_{i=1}^{N} d_i L_i F_i$$
(7)

Subject to,

$$\sum_{k=1}^{V} \sum_{j=1}^{N} x_{ijk} = 1 ; \forall i \in \mathbb{N}$$

$$\tag{8}$$

$$\sum_{i=1}^{N} d_i \sum_{i=1}^{N} x_{iik} \le q_i ; \forall k \in V$$

$$\tag{9}$$

$$\sum_{i=1}^{N} x_{0ik} = 1, \forall k \in V \tag{10}$$

$$\sum_{i=1}^{N} x_{ihk} - \sum_{j=1}^{N} x_{hjk} = 0, \ \forall h \in \mathbb{N}, \forall k \in \mathbb{V}$$
 (11)

$$\sum_{i=1}^{N} x_{i,n+1,k} = 1, \forall k \in V$$
 (12)

$$x_{ijk} \in \{0,1\}, \ \forall i,j \in \mathbb{N}, \forall k \in V$$

$$\tag{13}$$

$$\sum_{i=1}^{N} d_i F_i \le W_i F_i; \ \forall i \in \mathbb{N}$$
 (14)

Objective function (7) is the cost of transportation and costs $3^{\rm rd}$ party logistics. It is the sum of multiplication of each move from vehicle k to position j (x_{ijk}) with transportation costs of moving from position i to position j (c_{ij}) and costs to using third party logistics for every request on a non-hub. According to El-Sherbeny [8], constraint (8) indicates there is only one vehicle that departs from position i to position j with vehicle k. Constraint (9) indicates that no vehicle is filled exceeding its capacity. Constraints (10-12) guarantee that each vehicle leaves node 0, then after arriving at the customer destination vehicle can leave again, and the vehicle eventually stops at node n + 1. Constraint (10) sums up the displacement of each vehicle V to go to position j from node 0 (x_{0jk}) and must be equal to one. Constraint (11) sums up each vehicle V departing from the initial position i towards the customer h then subtracting the number of each vehicle V departing from the customer h 'to the next position j (x_{hjk}) and must be 0. Constraint (13) is the integrality for the variable decision. This constraint ensures that the value of the displacement for each vehicle V from position i to position j always be worth one or zero. Constraint (14) is a limitation when third party logistics for the



second hub, which is a non-hub is not able to accommodate a number of items in the warehouse it owns, where di is a request on non-hubs.

2.3. The Data Collection

Capital for the construction of hubs owned by a company was 25,000,000,000 IDR. It was presumed that each hub has a requirement of 600 m² for the same location. The data was taken from www.rumah123.com. Each area of the different buildings were converted to the same area. Transportation cost for Long Box CDD truck vehicles was 150,000 IDR, and consumption cost was 12,000 IDR, the usage cost of a vehicle was Rp. 1,000,000, IDR and there are also revenues for each demand for 20,000 IDR. Table 1 is the distance between nodes in the distribution network generated by the Bing map. Table 2 gives the data on demand, cost of building hub, and warehouse capacity in third party logistics.

Table 1. Distance Between Nodes

	Jakarta	Bogor	Bandung	Banten	Bekasi	Depok	Kara- wang	Malang	Sura- baya	Tang- erang	Yogya- karta
Jakarta	0.00	59.95	152.97	109.13	21.62	41.69	82.64	865.16	798.24	29.28	550.02
Bogor	60.51	0.00	179.90	159.08	59.85	38.51	129.30	892.10	825.17	79.23	576.95
Bandung	157.01	181.90	0.00	258.86	133.78	163.64	172.52	812.57	745.65	179.01	401.39
Banten	109.91	161.20	256.69	0.00	136.58	130.21	206.09	968.88	901.96	92.46	653.74
Bekasi	23.36	58.89	136.51	136.17	0.00	40.64	68.28	848.71	781.79	56.32	533.56
Depok	43.13	26.55	162.52	129.55	42.47	0.00	111.92	874.72	807.80	49.70	559.57
Karawang	82.83	129.89	171.07	206.85	67.20	111.64	0.00	883.27	816.34	105.56	568.12
Malang	862.81	887.70	807.98	964.66	839.58	869.44	878.32	0.00	99.80	884.81	391.81
Surabaya	798.62	823.51	743.79	900.47	775.40	805.26	814.14	101.14	0.00	820.62	327.62
Tangerang	29.93	81.22	176.71	93.07	56.60	50.23	126.11	888.90	821.98	0.00	573.75
Yogyakarta	553.58	578.46	400.47	655.42	530.35	560.21	569.09	394.77	327.84	575.58	0.00

Table 2. Data

Hub	Demand (unit)	Cost of Building (Million IDR)	Warehouse Capacity (Unit)
Bogor	350	6,000	1,000
Bandung	800	6,546	1,500
Banten	250	$1{,}175$	1,250
Bekasi	600	4,320	1,600
Depok	450	6,600	1,450
Karawang	350	4,560	1,350
Malang	625	4,350	1,625
Surabaya	725	8,182	1,725
Tangerang	800	4,600	1,800
Yogyakarta	575	7,500	1,575

2.4. Implementation

In the implementation, it was assumed that a company can weigh more ondemand compared to distance. Therefore, the weight value for distance (Ω) was 0.2 and the weight for demand $(1-\Omega)$ was 0.8. The reason was that the companies have a preference to prioritize customer service compared to the distance that must be taken. In addition, demand data and mileage were assumed per year for calculations in equation (4). This problem was solved by using LINGO 17.0 x64 bit software.

3. Result and Discussion

The results of applying the problem into the research model determining the hub by considering the vehicle routing problem model, distance, and demand are as follows. There are five hubs chosen to be built, namely hubs in Bandung, Banten, Bekasi, Depok, and Tangerang. The total transportation costs and fees for third party logistics for nonhubs is 72,501,500 IDR. Moreover, the total cost of constructing the hub required is 21,201,000,000 IDR. The routing of the vehicle with a weight of 0.8 can be seen in Table 3 and Table 4. According to Jokar [32], requests that occur in an area depend on facilities in the area. We can see from Table 3 that the chosen hub has a big demand in weight value of 0-0.8.

To find out is the output model as expected and to know the optimal weight to minimize cost, the study carried out sensitivity analysis. There are two weights in determining the hub to be built. The weight of distance is the distance between the distribution center to the hub, and the weight of demand is the total number of demand on a hub. In this test, weight changes see the response to the model results from 0 to 1 with incremental of 0,1, and the result in Table 3.

Table 3. Result of Weight Sensitivity Analysis

Weight Value			Amount of	Total of	
Distance	Demand	Location of Built Hub	Capital Req. (1,000,000) IDR	Transportation Cost (10,000) IDR	
0	1	Bandung. Banten. Malang. Surabaya dan Tangerang	23,888.00	9,081.3	
0.1	0.9	Bandung. Banten. Bekasi. Surabaya dan Tangerang	23,888.00	8,878.14	
0.2	0.8	Bandung. Banten. Bekasi. Surabaya dan Tangerang	23,888.00	8,878.14	
0.3	0.7	Bandung. Banten. Bekasi. Surabaya dan Tangerang	24,376.00	8,878.14	
0.4	0.6	Bandung. Banten. Bekasi. Depok dan Tangerang	21,201.00	7,250.15	
0.5	0.5	Bandung. Banten. Bekasi. Depok dan Tangerang	21,201.00	7,250.15	
0.6	0.4	Bandung. Banten. Bekasi. Depok dan Tangerang	21,201.00	7,250.15	
0.7	0.3	Bandung. Banten. Bekasi. Depok dan Tangerang	21,201.00	7,250.15	
0.8	0.2	Bandung. Banten. Bekasi. Depok dan Tangerang	21,201.00	7,250.15	
0.9	0.1	Bogor Banten. Bekasi. Depok dan Tangerang	21,255.00	7,085.19	
1	0	Bogor Banten. Bekasi. Depok dan Tangerang	22,695.00	7,085.19	

Table 3 explains the amount of capital needed and the estimation of the overall transport costs. When the weight values are at (distance) 0.1-0.3, there is a disparity in the range compared to the value of the previous weight. There are variations in the ranking between or before the values of the weights. Weight values at (distance) 0.4-0.8 give a difference in the range as compared to the value of the previous weight. There is a difference in the rating between the weight values or the previous one. The last with a weight value of 0.9-1 discrepancy exists as compared to the value of the previous weight. There is a disparity in rating between the value of the weight or the previous one. It concluded that there are four variations in the range of hubs that established when



changes in weight values occur. The optimal routing presented in Table 4. Routing determination for assigned vehicles from the distribution center to each hub and non-hub is performed separately.

Table 4. Routing

Weight	Vehicle	Hub Route	Non-Hub Route		
	1	Jakarta - Banten – Jakarta	Jakarta - Karawang - Bogor - Tangerang - Jakarta		
0 - 0.1	2	Jakarta - Bekasi - Depok – Jakarta	Jakarta - Jogyakarta - Bandung - Jakarta		
	3	Jakarta - Surabaya - Malang – Jakarta	-		
0.2 - 0.3	1	Jakarta - Bekasi - Banten - Tangerang - Jakarta	Jakarta - Depok - Bogor - Jakarta		
	2	Jakarta - Bandung - Surabaya – Jakarta	Jakarta - Yogyakarta - Malang - Karawang -Jakarta		
0.4 - 0.8	1	Jakarta - Bekasi - Banten - Tangerang - Jakarta	Jakarta - Bogor - Kawarang - Jakarta		
	2	Jakarta - Bandung - Depok – Jakarta	Jakarta - Jogyakarta - Surabaya - Malang - Jakarta		
0.9 - 1	1	Jakarta - Bekasi - Depok - Bogor - Jakarta	Jakarta - Bandung - Karawang - Jakarta		
	2	Jakarta - Banten - Tangerang – Jakarta	Jakarta - Jogyakarta - Surabaya - Malang - Jakarta		

4. Conclusions

The mathematical model in determining the location of hubs by considering distance, demand, and investment has developed with the route to minimize transportation costs. Proposed model effective to minimize transportation cost According to the case above, the ideal distance weight suggested for the problem is to use a distance weight of 0.9-1 with the smallest capital cost needed. Nevertheless, this weight is only a choice for a company to increase profits based on reducing overall transport costs and expenditure. There are a few avenues for further study. Next, adding additional criteria for creating hubs, such as legislation, work ethic, and others, would be an exciting subject to be explored. Second, the introduction of a penalty fee where third party logistics cannot satisfy all requests to make the model more realistic.

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